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METHOD OF APPROXIMATE CALCULATION OF AERODYNAMIC CHARACTERISTIC--ETC(U)

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METHOD OF APPROXIMATE CALCULATION OF AERODYNAMIC CHARACTERISTICS OF CAMBERED WINGS WITH VARIABLE SWEEP

by

A. I. Pastukhov



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METHOD OF APPROXIMATE CALCULATION OF AERODYNAMIC CHARACTERISTICS OF CAMBERED WINGS WITH VARIABLE SWEEP

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Block	Italic	Transliteration	Block	Italic	Transliteration
А а	А а	А, a	Р р	Р р	Р, r
Б б	Б б	В, b	С с	С с	С, s
В в	В в	В, v	Т т	Т т	Т, t
Г г	Г г	Г, g	У у	У у	У, u
Д д	Д д	Д, d	Ф ф	Ф ф	Ф, f
Е е	Е е	Ye, ye; Е, e*	Х х	Х х	Kh, kh
Ж ж	Ж ж	Zh, zh	Ц ц	Ц ц	Ts, ts
З з	З з	Z, z	Ч ч	Ч ч	Ch, ch
И и	И и	I, i	Ш ш	Ш ш	Sh, sh
Й й	Й й	Y, y	Щ щ	Щ щ	Shch, shch
К к	К к	К, k	Б ъ	Б ъ	"
Л л	Л л	L, l	Н ъ	Н ъ	Y, y
М м	М м	M, m	Б ъ	Б ъ	"
Н н	Н н	N, n	Э э	Э э	E, e
О о	О о	O, o	Ю ю	Ю ю	Yu, yu
П п	П п	P, p	Я я	Я я	Ya, ya

*ye initially, after vowels, and after ъ, ъ; е elsewhere.
When written as ё in Russian, transliterate as yё or ё.

RUSSIAN AND ENGLISH TRIGONOMETRIC FUNCTIONS

Russian	English	Russian	English	Russian	English
sin	sin	sh	sinh	arc sh	\sinh^{-1}
cos	cos	ch	cosh	arc ch	\cosh^{-1}
tg	tan	th	tanh	arc th	\tanh^{-1}
ctg	cot	cth	coth	arc cth	\coth^{-1}
sec	sec	sch	sech	arc sch	\sech^{-1}
cosec	csc	esch	esch	arc esch	\esch^{-1}

Russian	English
rot	curl
lg	log

METHOD OF APPROXIMATE CALCULATION OF AERODYNAMIC CHARACTERISTICS OF
CAMBERED WINGS WITH VARIABLE SWEEP

A. I. Pastukhov, Department of Hydromechanics

The wing is replaced by a system of attached vortices of variable intensity over the span, distributed continuously over its middle surface. Emerging from each point on the vortex surface are free rectilinear vortices with variable angles of decalage over the chords and span and arranged in the vertical plane parallel to the root section.

In calculating inductive velocities the system of attached vortices is assumed to be equivalent to the vortex system of the

projection of the middle surface onto the plane which passes through its root chord in a direction parallel to the span.

The angle of sweep of the i -th portion of the attached vortex (Fig. 1) is determined by the expression

$$\operatorname{tg} \chi_i(x) = \operatorname{tg} \chi_v^* - \bar{x} \operatorname{tg} \chi_v^{**},$$

where

$$\operatorname{tg} \chi_v^* = \frac{1}{2} (\operatorname{tg} \chi_{vv} + \operatorname{tg} \chi_{vv}); \operatorname{tg} \chi_v^{**} = \frac{1}{2} (\operatorname{tg} \chi_{vv} - \operatorname{tg} \chi_{vv}),$$

$\bar{x} = \frac{x}{a}$ is the relative coordinate of an elementary lifting vortex in the root section.

Assuming that the vortex density $\bar{J}(x_{vv}, \alpha)$ at section point x_{vv} and in the root section $\bar{J}(x, \alpha)$ are related by distributing function $\bar{J}(x_{vv}, \alpha)$ in the form of

$$J(x_{vv}, \alpha) = \bar{J}(x_{vv}, \alpha) J(x, \alpha) \quad (1)$$

for the intensity of the elementary lifting and free vortices we can get, accordingly,

$$\left. \begin{aligned} & J(x, \alpha) \bar{J}(x_{vv}, \alpha) \bar{a}_{vv} \cos \chi_v dx \\ & J(x, \alpha) \left[\frac{\partial \bar{J}(x_{vv}, \alpha)}{\partial x} \bar{a}_{vv} + \bar{J}(x_{vv}, \alpha) \frac{\partial \bar{a}_{vv}}{\partial x} \right] \cos \chi_v dx dz \end{aligned} \right\},$$

where local narrowing of the wing projection is determined by expressions

$$\tilde{a}_{vv} = \frac{a_{vv}}{a} = \tilde{a}_v - \left(\tilde{x} \tilde{L} - \sum_{i=0}^{n-1} \tilde{L}_i \right) \operatorname{tg} x_v^*; \quad \tilde{a}_v = \frac{a_v}{a}; \quad \tilde{x} = \frac{x}{L}; \quad \tilde{L}_i = \frac{L_i}{a}; \quad \tilde{L} = \frac{L}{a}.$$

For calculating inductive velocities the v -th segment of the span is broken down into n , bands of width L_v/n_v . Quantities $\partial \tilde{Y}_{vi}/\partial x$, $\tilde{a}_{vv} = \tilde{a}_{vi}$, β_{vi} are assumed to be constant and equal to their values in the middle i , of the bands. In this case, after switching to angular coordinate

$$x = -\cos \theta; \quad \tilde{x}_{vi} = -\tilde{a}_{vi} \cos \theta$$

for the normal velocity component of the downwash, caused by the free vortices at the point with coordinates

$$x'_{vv} = -a \cos \theta'; \quad x'_{vv} = \sum_{i=0}^{n-1} L_i + (x_v + 0.5) \frac{L_v}{n_v}$$

we get, approximately:

$$W_{vv}^{(n)} = \frac{p_{vv}^*}{2\pi} \int_{-\pi}^{\pi} Y_{vv} \sin \theta d\theta = \frac{1}{4\pi} \int_{-\pi}^{\pi} \left\{ Y_{vv} \frac{\sin \theta}{\tilde{Y}_{vv} \tilde{L}} \sum_{i=0}^{n-1} \tilde{L}_i \cos x \left[\sum_{i=0}^{n-1} \frac{\partial \tilde{Y}_{vi}}{\partial x} \tilde{a}_{vi} (\varphi + \varphi') \cos \beta_{vi} \right] \right\} d\theta, \quad (2)$$

where

$$\varphi(\varphi) = \frac{\tilde{L} (\tilde{x}_{vi} + \tilde{x}'_{vv})}{\theta' \sin \beta_{vi} + [\tilde{L} (\tilde{x}_{vi} + \tilde{x}'_{vv})]^2} \left(1 + \frac{\theta \cos \beta_{vi}}{\sqrt{\theta'^2 + [\tilde{L} (\tilde{x}_{vi} + \tilde{x}'_{vv})]^2}} \right); \quad x_{vi} = \sum_{i=0}^{n-1} L_i + (i_v + 0.5) \frac{L_v}{n_v}, \quad (3)$$

$$\theta = \tilde{x}'_{vv} - \tilde{x}_{vi} - \tilde{L} (\tilde{x}_{vi} \operatorname{tg} x_v^* - \tilde{x}'_{vv} \operatorname{tg} x_v^*) \cdot \left(\sum_{i=0}^{n-1} \tilde{L}_i \right) \operatorname{tg} x_v^* - \sum_{i=0}^{n-1} \tilde{L}_i \operatorname{tg} x_v^* + \left(\sum_{i=0}^{n-1} \tilde{L}_i \right) \operatorname{tg} x_v^*. \quad (4)$$

The velocity component of the downwash $W_{\text{ext}}^{(2)}$ is calculated by (2)-(4), replacing $\cos \beta_{\text{ext}}$ in (2) by $\sin \beta_{\text{ext}}$; the component $W_{\text{ext}}^{(3)}$ is calculated by replacing $(\varphi + \varphi') \cos \beta_{\text{ext}}$ by $(\varphi + \varphi') \sin \beta_{\text{ext}}$, where

$$\varphi'(\varphi') = \left\{ \frac{\vartheta}{\vartheta' \sin \beta_{\text{ext}} + \varphi'(\varphi')^2} \left(1 + \frac{\vartheta \cos \beta_{\text{ext}}}{\sqrt{\vartheta' + \varphi'(\varphi')^2}} \right) \right\}.$$

$$\varphi(\varphi') = \sum_{i=0}^{n-1} \bar{L}_i + \sum_{i=0}^{n-1} \bar{L}_i + (i + 0.5) \frac{\bar{L}_x}{n_y} + (k_x + 0.5) \frac{\bar{L}_x}{n_x}$$

By using the same assumptions for the velocity caused by the attached vortices, we can get

$$W_{\text{ext}} = \frac{p_{\text{ext}}^*}{2\pi} \int_0^{\pi} \frac{Y_{\text{ext}} \sin \theta}{\cos \theta - \cos \theta'} d\theta = \frac{1}{4\pi} \int_0^{\pi} \left\{ Y_{\text{ext}} \frac{\sin \theta}{\bar{Y}_{\text{ext}}} \sum_{i=0}^{n-1} \frac{\bar{L}_i}{n_y} \cos \bar{z}_i \left[\sum_{i=0}^{n-1} \bar{a}_{i1} \bar{L}_{ni} (H + H') \right] \right\} d\theta,$$

where

$$H(H') = \frac{\vartheta + \varphi(\varphi') \lg z_v}{\sqrt{[\vartheta' + \varphi'(\varphi')]^2}}.$$

In compiling the integral equation the velocities which are normal to the wing projection are considered to be directed along the local normals (n_{ext} in Fig. 2) to the middle surface. Then, the condition of impermeability is written in the form of

$$\frac{p_{\text{ext}}^*}{2\pi} \int_0^{\pi} \frac{Y_{\text{ext}} \sin \theta d\theta}{\cos \theta - \cos \theta'} = V_{\infty} \sin \alpha_{\text{ext}}^* \cos \psi_{\text{ext}} - \frac{p_{\text{ext}}^*}{2\pi} \int_0^{\pi} Y_{\text{ext}} \sin \theta d\theta, \quad (5)$$

where

$$\alpha_{\text{ext}}^*(\theta', \alpha) = \alpha + \alpha_{\text{ext}} + \alpha_{\text{ext}}(\theta'),$$

α is the angle of attack of the plane of the wing projection;

α_{ext} - angle of twist of the middle section of the k -th plane in relation to the root section;

$\alpha_{\text{ext}}(\theta')$ - angle of curvature of middle line of section;

$\psi_{\text{ext}}(\theta')$ - angle between local normal and plane $O_{\text{ext}}x_{\text{ext}}y_{\text{ext}}$.

If we seek the solution to (5) in the form of a series [3], [4].

[5]

$$Y_{\text{ext}}^*(\theta, \alpha) = \frac{Y_{\text{ext}}(\theta, \alpha)}{V_{\infty}} = 2 \left[A_{\text{ext}}(\alpha) \operatorname{ctg} \frac{\theta}{2} + \sum_{m=1}^{\infty} A_{m\text{ext}}(\alpha) \sin m\theta \right], \quad (6)$$

we can get

$$A_{\text{ext}} = \frac{1}{\pi} \left(\int_0^{\pi} \bar{P}_{\text{ext}} \sin \alpha_{\text{ext}}^* \cos \psi_{\text{ext}} d\theta' - R_{\text{ext}} \int_0^{\pi} \bar{P}_{\text{ext}}^* d\theta' \right),$$

$$A_{m\text{ext}} = \frac{1}{\pi} \left(\int_0^{\pi} \bar{P}_{\text{ext}} \sin \alpha_{\text{ext}}^* \cos \psi_{\text{ext}} \cos m\theta' d\theta' - R_{\text{ext}} \int_0^{\pi} \bar{P}_{\text{ext}}^* \cos m\theta' d\theta' \right),$$

$$R_{\text{ext}} = \frac{\int_0^{\pi} \bar{P}_{\text{ext}}^* (1 - \cos \theta') \sin \alpha_{\text{ext}}^* \cos \psi_{\text{ext}} d\theta'}{\pi + \int_0^{\pi} \bar{P}_{\text{ext}}^* (1 - \cos \theta') d\theta'}; \quad \bar{P}_{\text{ext}}^* = \frac{P_{\text{ext}}^*}{P_{\text{ext}}}; \quad \bar{P}_{\text{ext}}^* = \frac{1}{P_{\text{ext}}^*}.$$

As our original values of P_{ext}^* and P_{ext} we can use those calculated for determining vortex density over the chord by the law of the

cotangent with an elliptical distributing function. The value of the angle $\beta_v(\theta, \alpha)$ can be assumed constant (according to [3] $\beta_v = \alpha$, according to [1] $\beta_v = \frac{\alpha}{2}$).

From the obtained values of A_{xx} and A_{yy} we determine according to (1) and (6) the distributing function of the first approximation and also P_{xx}' and P_{yy}' for distribution of vortex density (6) with the variability of values $\beta_v(\theta, \alpha)$ considered.

We know that the most intensive formation of free vortices occurs on the leading lateral edges. The angle of slope of the vortices to the lifting surface on these sections can be determined approximately in the form of

$$\operatorname{tg} \beta_{xx}(\theta, \alpha) = \frac{\sin \alpha_{xx}^*}{\cos \alpha_{xx}^* + \left(A_{xx} + \frac{1}{2} A_{yy} \right) P_{xx}' + \frac{1}{2} l_{xx}^* \cos \lambda_{xx}}. \quad (7)$$

The boundaries of the sections where intensive vortex formation occurs are very difficult to define. Moreover, inside the boundary layer, with the exception of the wing surface itself, the velocities normal to it are generally equal to zero and the flow lines do not adjoin the surface. On this basis we assume the possibility of directing the axes of the free vortices along these flow lines and consider the angles of slope of the free vortices not equal to zero even beyond the limits of the section, where such a branching of the

vortices is confirmed experimentally.

If we assume that the distributing functions differs little from the elliptical and, consequently, the deciding role in the formation of the downwash is played by vortices of great intensity flowing off the tip sections, then there can be no great error in "spreading" angle β , determined by expression (7), over the entire wing surface. This assumption does not contradict the condition of nonleakage, since the vortex system is actually formed in the boundary layer and only for the calculation schematic is it taken to the middle surface.

The second and subsequent approximations continue until the values of the coefficients of the series coincide within the limits of assigned calculation accuracy.

For a small number of breaks in the leading and trailing edges of the wing the calculation can be reduced to solving a system of algebraic equations, which has definite advantages for digital computer calculation. With this in mind, after introducing the symbols

$$M_i = \frac{\tilde{L}_i \tilde{a}_{vi}}{2 n_i \tilde{L}} (\varphi + \varphi') \cos \beta_{vi} \cos \chi_v; \quad M = \frac{\tilde{L}_v \tilde{a}_{vi}}{2 n_v} (H + H') \cos \chi_v,$$

we can write equation

$$\int \sum_{n=0}^{\infty} \sum_{i=0}^{n-1} \left[\gamma_{vi}^* (M + n_v M_i) - \gamma_{v+1,i}^* n_v M_i \right] \sin \theta d\theta = 2\pi i \sin \alpha_{\infty}^* \cos \psi_{\infty}, \quad (8)$$

where

$$\gamma_{vi}^* = \gamma_{v+1,0}^*, \quad \gamma_{v+1,n}^* = -2\gamma_{v+1,n-1}^*.$$

If we substitute in (8) the value γ_{vi}^* from (6) and confine ourselves to the number of q terms of the series, we can get an equation for $(q+1) \sum_{n=0}^{\infty} n_v$ of coefficients A_{vvi} and A_{mv1} ($m=1 \div q$). Given $q+1$ by quantities θ^* for each of the values of $\kappa_r = 0 \div n_{\infty} - 1$ ($\kappa=0 \div \mu-1$) we can also obtain the corresponding number of algebraic equations which are linear with respect to the coefficients of series (6).

If we assume that the downwash velocity components $W_{\infty \kappa}^{z(x)}$ are directed in planes tangent to the middle surface of the wing, then for the component of total relative velocity normal to the axis of the vortex, we get

$$\bar{V}_{\infty \kappa} = \frac{V_{\infty \kappa}}{V_{\infty}} = (\cos \alpha_{\infty}^* + \bar{W}_{\infty \kappa}^{(x)}) \cos \chi_{\infty \kappa} - \bar{W}_{\infty \kappa}^{(x)} \sin \chi_{\infty \kappa}.$$

In this case the coefficients of the force of the pressure of the κ_r -th section normal to the plane of the projection (direction $n_{\infty \kappa}$ in Fig. 2) referred to an element of the projection surface $2a_{\infty \kappa} dx'$, is found in the form of

$$(C_n)_{\infty \kappa} = \int_0^{\pi} \gamma_{\infty \kappa}^* (\theta', \alpha) \frac{V_{\infty \kappa}(\theta', \alpha)}{\cos \chi_{\infty \kappa}(\theta')} \sin \theta' d\theta', \quad (9)$$

however, the expressions $(c_y)_{\epsilon\epsilon}$ and $(c_x)_{\epsilon\epsilon}$ are found by multiplying the integrand function (9) by

$$\frac{\cos \alpha_{\epsilon\epsilon}^*}{\cos(\alpha_{\epsilon\epsilon} + \alpha_{\epsilon\epsilon})} \text{ and } \frac{\sin \alpha_{\epsilon\epsilon}^*}{\cos(\alpha_{\epsilon\epsilon} + \alpha_{\epsilon\epsilon})} \text{ respectively.}$$

For the coefficient of the moment of hydrodynamic forces relative to the axis running through the leading edge of the root section parallel to the stand, we get

$$(m_x)_{\epsilon\epsilon} = \frac{1}{2} \left\{ (C_n)_{\epsilon\epsilon} \left[1 + \frac{1}{\tilde{a}_{\epsilon\epsilon}} \left(\sum_{\epsilon=0}^{n-1} \tilde{L}_\epsilon \operatorname{tg} \chi_\epsilon + \tilde{L}_\epsilon \frac{\kappa + 0.5}{n_\epsilon} \operatorname{tg} \chi_{n_\epsilon} \right) \right] \right\} -$$

$$- \int_0^{\pi} Y_{\epsilon\epsilon}^*(\theta', \alpha) \frac{V_{\epsilon\epsilon}(\theta', \alpha)}{\cos \chi_{\epsilon\epsilon}(\theta')} \left\{ \cos \theta' + \tilde{y}_{\epsilon\epsilon}(\theta') \operatorname{tg} [\alpha_{\epsilon\epsilon} + \alpha_{\epsilon\epsilon}(\theta')] \right\} \sin \theta' d\theta'.$$

If we assume that these coefficients are constant within the limits of the κ -th band, then the integral characteristic can be obtained in the form of

$$C_y = \frac{2 \sum_{\epsilon=0}^{n-1} \tilde{L}_\epsilon \left[\sum_{\epsilon=0}^{n-1} (C_y)_{\epsilon\epsilon} \tilde{a}_{\epsilon\epsilon} \right]}{\sum_{\epsilon=0}^{n-1} (\tilde{a}_{\epsilon-1} + \tilde{a}_\epsilon) \tilde{L}_\epsilon} ; \quad m_x = \frac{2 \sum_{\epsilon=0}^{n-1} \tilde{L}_\epsilon \left[\sum_{\epsilon=0}^{n-1} (m_x)_{\epsilon\epsilon} \tilde{a}_{\epsilon\epsilon} \right]}{\sum_{\epsilon=0}^{n-1} (\tilde{a}_{\epsilon-1} + \tilde{a}_\epsilon) \tilde{L}_\epsilon} ,$$

where $\tilde{a}_{\epsilon-1}$ represents the narrowing at the beginning of the ζ -th section, \tilde{a}_ϵ - at the end.

The calculations of the first approximation, performed according

to the discussed method for a plane triangular wing, are in good agreement with the data of the experiment (Fig. 3).

Figure 4 gives us an idea of the distributing function and the distributed hydrodynamic characteristics.

References

1. Bollay, W. A Nonlinear Theory and its Application to Rectangular Wing of Small Aspect Ratio. - ZAMM, 1939.
2. Bartlett, G., Windal, R. Experimental Investigation on Influence of Edge Shape on the Aerodynamic Characteristics of Low-Aspect Ratio Wings at Low Speeds. - Cornell Aeronaut. Lab. Rept., No. 62, 1954.
3. Polyakhov, N. N., Pastukhov, A. I. Theory of Lifting Surface of Rectangular Shape. - Herald of Leningrad State University, No. 13, 1959.
4. Polyakhov, N. N., Pastukhov, A. I. Vortex Theory of Lifting Surface. - Herald of Leningrad State University, No. 19, 1968.

S. Pastukhov, A. I. Nonlinear Theory of Wing of
Nonrectangular Plan Shape with Cambered Middle Surface. -
Transactions of Leningrad Institute of Aviation
Instruments, No. 66, Issue 2, 1969..

Fig. 1. Angles of sweep of wing and attached vortices.

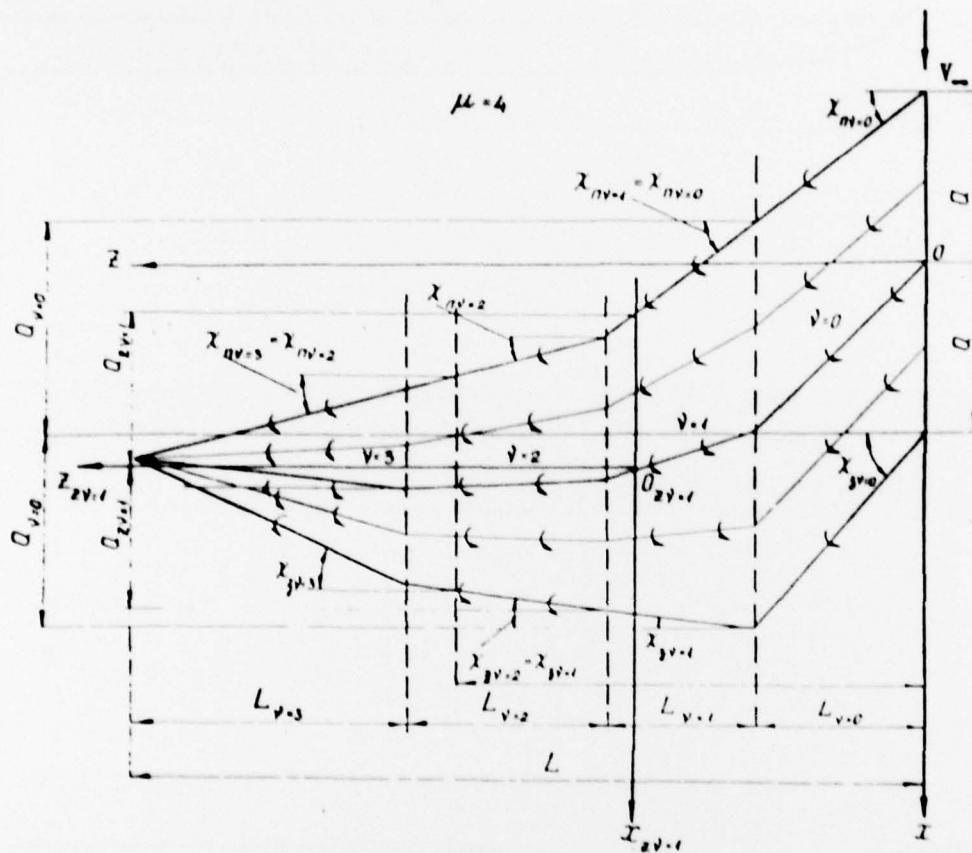


Fig. 2. Coordinate system of wing section. KEY: (1) Middle line of ζ -th section, (2) Projection plane.

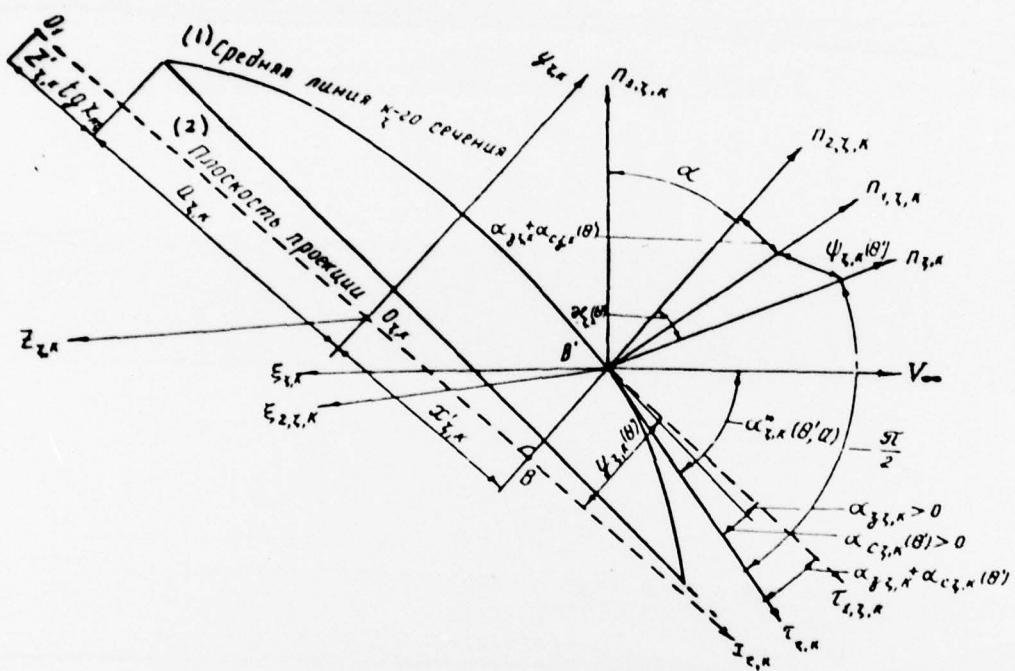


Fig. 3. Comparison of calculated results with experimental. KEY: (1) Calculation, (2) Sharp edges, (3) Round and elliptical edges, (4) Bartlett and Vidal, (5) Triangular wing $\lambda = 2$.

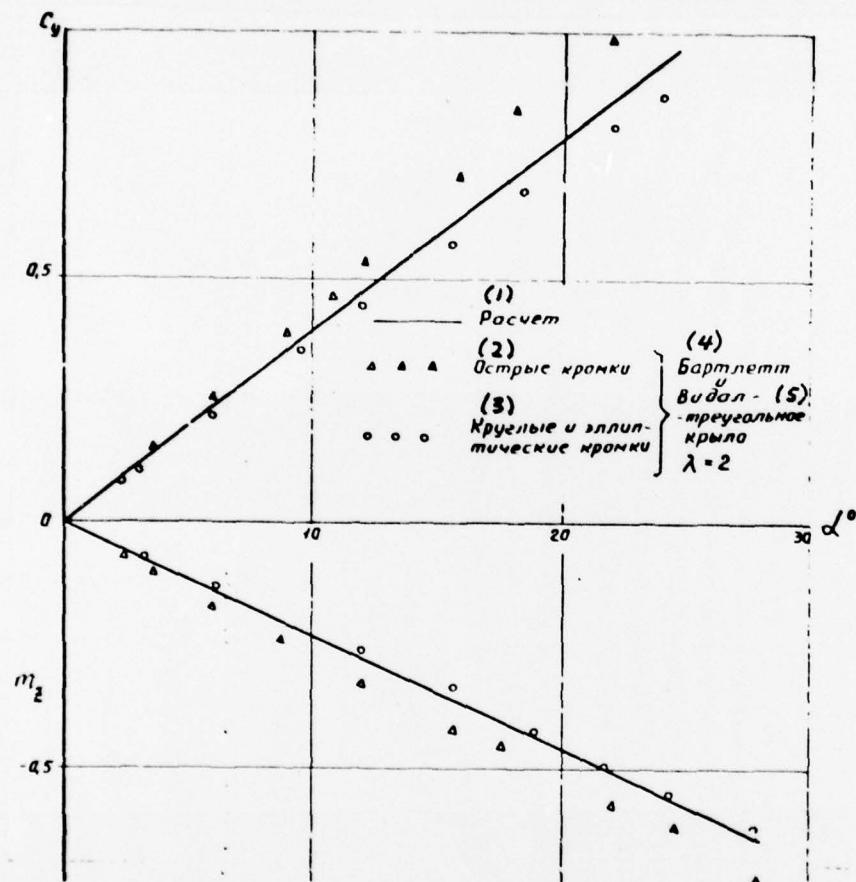
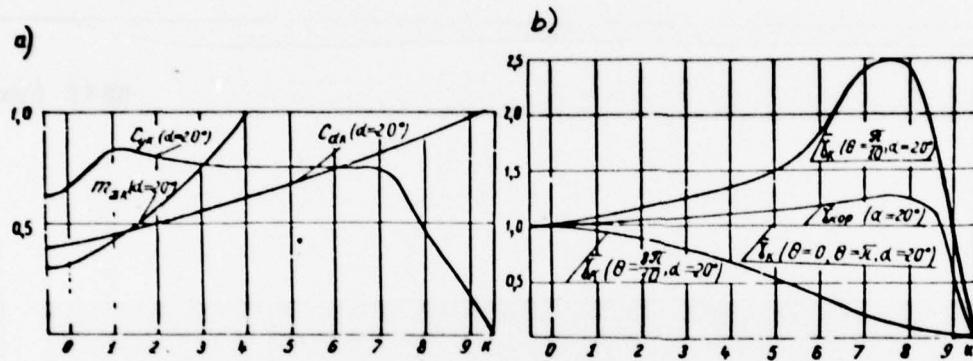


Fig. 4. Calculated values: a - of distributed hydrodynamic characteristics, b - of distributing function.



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